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Analysis of Sensor and Fusion Schedules of a Time-Triggered Sensor Fusion System

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Abstract—In this paper we analyze the sensor and fusion schedules of a time-triggered, Kalman filter based, multi-sensor fusion system. The fusion system is used as an environmental perception platform for advanced driver assistance systems and delivers its service to a safety related application. As the application demands cyclic updates with bounded accuracy, the influence of the sensor and fusion schedules on the service accuracy is analysed, which enables us to optimize the system without model dependent simulations.

I. INTRODUCTION

Multi-sensor data fusion systems are the enabling technology for advanced driver assistance systems. New features like adaptive cruise control with active steering, lane departure alert, parking pilot, and automatic emergency brake will be standard in the next car generation as electronic stabilization systems and anti lock braking systems are at present.

This paper deals with the optimization of a time-triggered, Kalman filter based, sensor fusion system for driver assistance systems consisting of two sensors, a bus system and a fusion/prediction core. It tracks objects and is supposed to deliver a real time image (model) of the environment at fixed intervals with bounded accuracy to a safety related application.

The rest of the paper is structured as follows: In section II the system set-up is described. In section III out of sequence measurement (OOSM) treatment strategies are discussed. Section IV discusses the overall system response time. We analyse the system schedule in section V. In section VI a conclusion is drawn.

II. SYSTEM DESCRIPTION

We consider a system with two identical sensors that measure the states of surrounding objects and transmit this information via a time-triggered bus system to a fusion/prediction core. The fusion/prediction core fuses the incoming information and then predicts the fused object states to real time as demanded by the safety related application (see figure 1). We use the following definitions:

- the cycle time t_C of a process is the time interval that this process requires for completion of its service while the start of two consecutive processes is t_C apart
- the execution time t_T of a process is the time interval in which this process completes its service where the start of two consecutive processes can be more than t_T apart

• the phase *t_P* of a process is defined as the time interval between the start of this process relative to the start of the first cycle of sensor 1

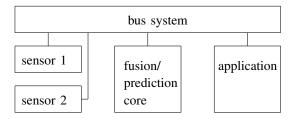


Fig. 1. Sensor fusion system

The two sensors have cycle times t_C^{sens1} and t_C^{sens2} that are identical to their preprocessing times and therefore adjustable by the choice of the speed of the sensor's processor. They deliver their measurement states $\vec{z}_{t_k}^{sens1}$ and $\vec{z}_{t_k}^{sens2}$ (with constant covariance matrices $R_{t_k}^{sens1}$ and $R_{t_k}^{sens2}$) over a time-triggered bus system to a fusion/prediction core. The bus system uses time division multiple access (TDMA) with fixed cycle time t_C^{tta} (the bus is not exclusively used by the sensor fusion system, hence the cycle time is assumed to be determined by external constraints). At the fusion/prediction core the information is processed in order to establish a robust image of the environment.

In figure 2 all cycle times t_C , process execution times t_T and phases t_P , relative to sensor 1, of sensor preprocessing $(t_C^{sens1}, t_C^{sens2}, t_P^{sens})$, measurement transmission $(t_C^{tta}, t_P^{tta1}, t_P^{tta2})$ and generation of the application update $(t_C^{pre}, t_T^{pre} \text{ and } t_P^{pre})$ that are processed within the fusion system are visualized.

To process the incoming measurements at the fusion/prediction core, we use a Kalman filter approach as described in [1]. As the Kalman filter is a widely used and well known algorithm for tracking moving targets, we will only give a short overview of the notation used throughout this paper. The estimated state vector of the tracked object $\hat{x}(t_{k-1}|t_{k-1})$ is updated with measurements at discrete points in time t_k . The state prediction from t_{k-1} to t_k is given by $\hat{x}(t_k|t_{k-1}) = F(t_k - t_{k-1}) \cdot \hat{x}(t_{k-1}|t_{k-1})$. The predicted state covariance matrix is computed as $P(t_k|t_{k-1}) = F(t_k - t_{k-1}) \cdot P(t_{k-1}|t_{k-1}) \cdot (F(t_k - t_{k-1}))^T + Q_{t_{k-1}}$. The measurement update of the predicted system state is $\hat{x}(t_k|t_k) = \hat{x}(t_k|t_{k-1}) + K_{t_k} \cdot \vec{v}_{t_k}$ with $K_{t_k} = P(t_k|t_{k-1}) \cdot H_{t_k}^T \cdot (H_{t_k}P(t_k|t_{k-1})H_{t_k}^T + R_{t_k})^{-1}$, $\vec{v}_{t_k} = \vec{z}_{t_k} - \hat{z}_{t_k}$ and $\hat{z}_{t_k} = H_{t_k} \cdot \hat{x}(t_k)$. The update of the covariance matrix is given by $P(t_k|t_k) = (I - K_{t_k} \cdot H_{t_k})^T + K_{t_k} \cdot R_{t_k} \cdot K_{t_k}^T$. The fusion/prediction core processes a measurement within t_T^{fus} .

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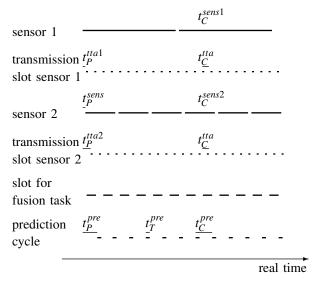


Fig. 2. System schedule

III. OUT-OF-SEQUENCE MEASUREMENT TREATMENT

In multi-sensor tracking systems, information about the same object can arrive out of sequence [2], [3], that means not in chronological order. Often, OOSM behavior is caused by an indeterministic transmission system, where the transmission time of a message may vary so much that a message from a later measurement may overtake a newer measurement. Such behavior is caused by transmission protocols with many retries such as many Internet protocols (e. g., TCP/IP) or in networks with dynamic routing (Internet, wireless sensor networks).

However, even if communication protocols with deterministic behavior, such as time-triggered approaches like flexray [4], TTCAN [5], TTP [6], or TTP/A [7] are used, the OOSM problem may arise.

Figure 3 depicts a situation with an OOSM problem that is independent from communication system issues. Due to different preprocessing times the indicated measurement from sensor 2 is received earlier at the fusion core than the indicated measurement from sensor 1 although the measurement from sensor 2 is newer.

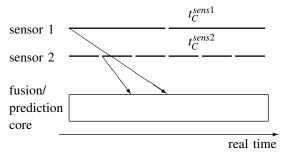


Fig. 3. Origin of out-of-sequence measurements

As the Kalman filter in the form of [1] can not handle OOSMs, architectural and algorithmic solutions have been developed.

Kaempchen et al. [8] use a measurement buffer between bus and fusion/prediction core. No measurement is delivered to the fusion/prediction core, before all measurements that have been sampled earlier have arrived at the buffer. Within the buffer the measurements are sorted chronologically. Kaempchen et al. further discuss the maximum latency (here defined as the time difference between the instant of the composition of the image representing the surrounding environment provided by sensor fusion and the bygone instant where this image was true) that arises between measurement recording and measurement fusion. It is distinguished between situations where only knowledge of the maximum measurement cycle times and situations where full knowledge of the measurement cycle times is available.

Another way to solve the OOSM problem are special algorithms which will be called "advanced algorithms" throughout this paper. These algorithms deal with one-lag and multi-lag delays, filtering and tracking, linear and non-linear systems as well as single-model and multi-model approaches [9], [10], [11], [12], [13], [14], [15], [16], [17], [18] and enable us to use the information of the faster sensor as soon as it is delivered to the fusion/prediction core.

For sake of discussion we will only consider the buffering approach as presented in [8] referred to as BUFF and the OOSM treatment algorithm Al1 of [10] referred to as ADVA.

IV. SYSTEM RESPONSE TIME

As the application is safety related, it expects to periodically receive (cycle time t_C^{pre}) real time object states with bounded accuracy. Due to the fact that the fused states always lag behind real time irrespective of the specific OOSM treatment applied, this image of the environment has to be predicted from state time t_{ST} to real time t_{RT} . The state time is the current time of the Kalman filter state and coincides with the measurement time of the latest fused (non-OOSM) sensor measurement, whereas real time is the actual physical time. The real time covariance matrix of the state can be determined by predicting the state time covariance matrix from state time t_{ST} to real time t_{RT} by $P(t_{RT}|t_{ST}) = F(t_{RT} - t_{ST}) \cdot P(t_{ST}|t_{ST}) \cdot (F(t_{RT} - t_{ST}))^T + Q_{ST}$.

As the dependence of $F(t_{RT} - t_{ST})$ and Q_{ST} on the prediction interval is well known for a given system, it is thus possible to consider the effect of the system parameters and the strategy for the treatment of OOSM (see also section III) on the overall system response time $(t_{RT} - t_{ST})$ as well as state time and real time covariance matrices of the state $(P(t_{ST}|t_{ST}))$ and $P(t_{RT}|t_{ST}))$.

With the overall system response time as $\Delta t = t_{RT} - t_{ST}$, $det(P(t_{RT}|t_{ST}))$ is given by

$$\det(P(t_{RT}|t_{ST})) =$$

$$\det(F(\Delta t) \cdot P(t_{ST}|t_{ST}) \cdot F(\Delta t)^{\top} + Q_{ST}) =$$

$$\det(P(t_{ST}|t_{ST})) + \Delta t \cdot P(t_{ST}|t_{ST}) (1,1) \cdot q +$$

$$O(\Delta t^{2})$$
(1)

This allows us to separate the influence of the sensor schedules and the OOSM treatment, which affect the state time covariance matrix $P(t_{ST}|t_{ST})$, and the influence of the bus, fusion and prediction schedules that affect the system

response time and such the covariance at real time $P(t_{ST}|t_{ST})$. From eq. 1 we see that, given $\det(P(t_{ST}|t_{ST}))$, the leading order increase of the covariance area at real time is linear in Δt . As will be demonstrated in section V, the variations in $P(t_{ST}|t_{ST})$ are negligible and it then suffices to minimize Δt in order to maximize the fusion accuracy at real time.

V. SYSTEM SCHEDULE

First we simulate the entire system at a given point in schedule parameter space. We use a simple dynamic system and measurement model in the fusion/prediction core (see appendix) and employ a Kalman filter (by linearization around a setpoint) as opposed to an extended Kalman filter as our estimation algorithm. As the computation of the covariance matrices of a Kalman filter is completely independent of the state and measurement vectors we need not input specific measurements and are thus independent of the actual driving situation. After convergence of the Kalman filter¹ the maximum of det($P(t_{RT}|t_{ST})$) is recorded. This constitutes one iteration of the optimization (minimization of det($P(t_{RT}|t_{ST})$)) over the regions of the schedule parameter space and we will discuss both the area of the covariance ellipse at state time det($P(t_{ST}|t_{ST})$) as well as at real time det($P(t_{RT}|t_{ST})$).

As t_C^{tta} and t_C^{pre} are fixed (see sections II and IV), t_C^{sens1} , t_C^{sens2} , t_T^{fus} and t_T^{pre} are the only system parameters whose modification changes the hardware of the system and affects such the overall system costs. In contrast, t_P^{sens} , t_P^{tta1} , t_P^{tta2} and t_P^{pre} can be modified without affecting the costs of the system by simply changing software parameters. We assume t_C^{tta} to be sufficiently small and will neglect t_C^{tta} , t_P^{tta1} and t_P^{tta2} in the further. That means that the preprocessed information is transmitted without further delay from the sensors to the fusion core. For every configuration of t_C^{sens1} , t_C^{sens2} , t_T^{fus} and t_P^{tre} , we choose t_P^{sens} and t_P^{pre} that minimize the maximum of det($P(t_{RT}|t_{ST})$) which has been computed numerically over a simulation time of 10 seconds ($t_{Sim} = 10 \ s$) performed with a simple dynamic system and measurement model (see appendix). t_T^{pre} is approximated by $t_T^{pre} \approx \frac{t_T^{fus}}{3}$. Note that all temporal parameters are varied in 1 ms steps.

In figure 4 we visualize the state time and real time accuracy for a given point in parameter space. We perceive, that the difference between the buffering and advanced algorithms approach for state time accuracy is negligible in comparison to the effects that are caused by prediction from state time to real time. Due to this the accuracy optimization can be achieved by evaluation of the minimum (by variation of the parameter space variables) of the maximum time difference between state time and real time that occurs within one macro period (least common multiple of all cycle-times) after the Kalman filter has converged.

For the buffering approach, we can describe the maximum of the interval $t_{RT} - t_{ST}$ (see figure 5) as maximum of the series t_{RT-ST}^{BUFF} i.m

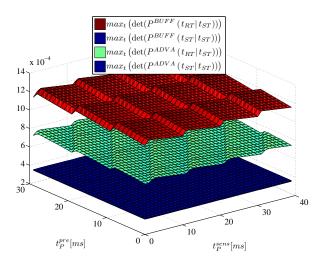


Fig. 4. State time and real time accuracy for $t_C^{sens1} = 130 \text{ ms}, t_C^{sens2} = 40 \text{ ms}$

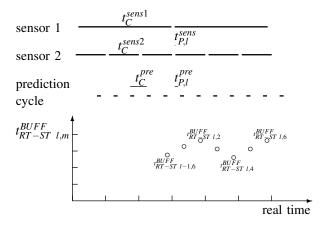


Fig. 5. $t_{RT-ST \ l,m}^{BUFF}$ profile

$$t_{RT-ST\ l,m}^{BUFF} = \begin{cases} (m-1)t_{C}^{pre} + t_{T}^{pre} + t_{P,l}^{pre} + t_{C}^{sens1} + \\ (1-n)\left(t_{C}^{sens2} - t_{P,l-1}^{sens1}\right) \\ \text{if } 0 \le n < 2 \\ (m-1)t_{C}^{pre} + t_{T}^{pre} + t_{P,l}^{pre} + \\ t_{C}^{sens1} + (2-n)t_{C}^{sens2} - t_{P,l-1}^{sens1} \\ \text{if } 2 \le n \end{cases}$$
(2)

with

K

$$l = 1, 2, \dots, \left\lfloor \frac{t_{Sim}}{t_C^{sens1}} \right\rfloor,\tag{3}$$

$$m = 1, 2, \dots, \left[\frac{t_C^{sens1} - t_{P,l}^{pre}}{t_C^{pre}}\right],$$
 (4)

$$n = \begin{cases} \min\left(\left\lfloor \frac{t_{P,l}^{pre}}{t_{T}^{fus}}\right\rfloor + (m-1) \left\lfloor \frac{t_{C}^{pre} - t_{T}^{pre}}{t_{T}^{fus}}\right\rfloor; \left\lceil \frac{t_{C}^{sens1} - t_{P,l-1}^{sens2}}{t_{C}^{sens2}}\right\rceil \right) \\ \text{if } t_{P,l}^{sens} \le t_{P,l}^{pre} - t_{T}^{fus} + (m-1) t_{C}^{pre} \\ \min\left(\left\lfloor \frac{t_{P,l}^{pre}}{t_{T}^{fus}}\right\rfloor + (m-1) \left\lfloor \frac{t_{C}^{pre} - t_{T}^{pre}}{t_{T}^{fus}}\right\rfloor; \left\lceil \frac{t_{C}^{sens1} - t_{P,l-1}^{sens2}}{t_{C}^{sens2}}\right\rceil + 1 \right) \\ \text{if } t_{P,l}^{sens} > t_{P,l}^{pre} - t_{T}^{fus} + (m-1) t_{C}^{pre} \end{cases}$$
(5)

¹Convergence of the Kalman filter here means that the covariance matrices have assumed a regular, periodic pattern. A constant steady state covariance matrix cannot be expected since the Kalman filter receives measurements from different sensors at different times.

$$t_{P,l}^{sens} = t_{P,l-1}^{sens} + \left[\frac{t_C^{sens1} - t_{P,l-1}^{sens1}}{t_C^{sens2}} \right] t_C^{sens2} - t_C^{sens1}$$
(6)

and

$$t_{P,l}^{pre} = t_{P,l-1}^{pre} + \left[\frac{t_C^{sens1} - t_{P,l-1}^{pre}}{t_C^{pre}} \right] t_C^{pre} - t_C^{sens1}$$
(7)

We consider the algorithmic overhead of the advanced algorithms in comparison to the simple buffering approach by adding a penalty term to $t_T^{fus} t_T^{fus} ADVA = t_T^{fus} + t_T^{Overhead 2}$ and can describe the maximum of the interval $t_{RT} - t_{ST}$ (see figure 6) as maximum of the series $t_{RT-ST}^{ADVA} o$

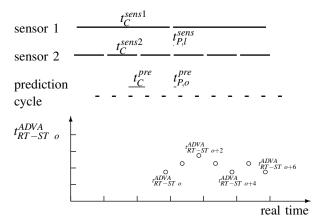


Fig. 6. $t_{RT-ST o}^{ADVA}$ profile

$$t_{RT-ST\ o}^{ADVA} = t_T^{pre} + t_{P,o}^{pre} + min\left(\left\lceil \frac{t_T^{fus}}{t_{P,o}^{pre}}\right\rceil; 2\right) t_C^{sens2} \qquad (8)$$

with

$$o = 1, 2, \dots, \left\lfloor \frac{t_{Sim}}{t_C^{sens2}} \right\rfloor \tag{9}$$

and

$$t_{P,o}^{pre} = t_{P,o-1}^{pre} + t_C^{pre} - \left[\frac{t_{P,o-1}^{pre} + t_C^{pre}}{t_C^{sens2}}\right] t_C^{sens2}$$
(10)

Visualization of $max_t (t_{RT} - t_{ST})_{BUFF} = max_{l,m} \left(t_{RT-ST \ l,m}^{BUFF} \right)$ and $max_t (t_{RT} - t_{ST})_{ADVA} = max_o \left(t_{RT-ST \ o}^{ADVA} \right)$ in figure 7 and comparison to figure 4 confirmes the connection between minimal prediction interval from state time to real time and optimal worst-case accuracy as stated above.

VI. CONCLUSION

We have performed the optimization of a sensor fusion system consisting of two sensors, a bus system and a fusion/prediction core with respect to the schedule parameter space $(t_C^{sens1}, t_C^{sens2}, t_P^{sens}, t_C^{pre}, t_T^{pre}$ and t_P^{pre}). The area of the covariance ellipse was chosen as the optimization criterion. We have shown that by a judicious choice of selected schedule

 $^{2}t_{T}^{Overhead}$ was empirically determined as $t_{T}^{Overhead} \approx t_{T}^{fus}$.

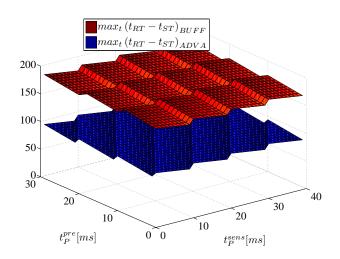


Fig. 7. $t_{RT} - t_{ST}$ [ms] for $t_C^{sens1} = 130$ ms, $t_C^{sens2} = 40$ ms

parameters that are adjustable at no or little cost the fusion accuracy can be improved. The time interval between the state time and the real time at which an application expects a new image of the environment was identified as the dominant factor on fusion accuracy. This means that for analytically tractable OOSM algorithms such as the buffering or advanced algorithms approach the optimization can be performed on the basis of the explicit formulae (which we have provided) without model dependent simulations.

APPENDIX

The example that is used in this paper corresponds to the one used in [10]. It is governed by the state transition matrix

$$F(t_{k+1} - t_k) = \begin{bmatrix} 1 & (t_{k+1} - t_k) \\ 0 & 1 \end{bmatrix}$$
(11)

where the state consists of position and velocity of one coordinate. The dynamical system is corrupted by a zeromean, white, discretized continuous time process noise with covariance matrix Q_{t_k}

$$Q_{t_k} = \begin{bmatrix} \frac{(t_{k+1}-t_k)^3}{3} & \frac{(t_{k+1}-t_k)^2}{2} \\ \frac{(t_{k+1}-t_k)^2}{2} & t_{k+1}-t_k \end{bmatrix} \cdot q$$
(12)

with $q = 0.5 \frac{m^2}{s^3}$ being the power spectral density of the continuous time process noise. The measurement matrix for both sensors is

$$H_{t_k}^{sensor1/2} = \begin{bmatrix} 1 & 0\\ 0 & 1 \end{bmatrix}$$
(13)

i. e. both position and velocity are assumed to be measurable. The measurement noise of both sensors is characterized by the diagonal covariance matrix

$$R_{l_k}^{sensor1/2} = \begin{bmatrix} 1m^2 & 0\\ 0 & 0.1\frac{m^2}{s^2} \end{bmatrix}.$$
 (14)

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